

## At Bishop Bronescombe C of E School our aim is:

1. We ALL start on the journey together



Some children will need additional support along the way.



3. **Some** children, who feel confident, will be let loose. They will be able to explore deeper into the woods before returning to the group, to continue on with the journey.



 Children will not be racing off ahead on a different journey.



Children will not be left behind, alone, isolated and disinterested.



 ALL children will have an adventure, taking small, incremental steps to get to the end learning point.

## Bishop Bronescombe calculation policy

The following pages show the Maths progression in calculation (addition, subtraction, multiplication and division) and how this works in line with the National Curriculum. The consistent use of the C-P-A; make it using equipment (concrete), draw it to explain (pictorial) and then use the calculation/formal methods (abstract) approach across Power Maths helps children develop mastery across all the operations in an efficient and reliable way. This policy shows how these methods develop children's confidence in their understanding of both written and mental methods. MASTERING MATHS is our aim for ALL of our children. All children are mathematicians; they just need to find the ways to help them.

## **KEY STAGE 2**

In upper Key Stage 2, children build on secure foundations in calculation, and develop fluency, accuracy and flexibility in their approach to the four operations. They work with whole numbers and adapt their skills to work with decimals, and they continue to develop their ability to select appropriate, accurate and efficient operations.

**Key language:** decimal, column methods, exchange, partition, mental method, ten thousand, hundred thousand, million, factor, multiple, prime number, square number, cube number

Addition and subtraction: Children build on their column methods to add and subtract numbers with up to seven digits, and they adapt the methods to calculate efficiently and effectively with decimals, ensuring understanding of place value at every stage.

Children compare and contrast methods, and they select mental methods or jottings where appropriate and where these are more likely to be efficient or accurate when compared with formal column methods.

Bar models are used to represent the calculations required to solve problems and may indicate where efficient methods can be chosen.

**Multiplication and division:** Building on their understanding, children develop methods to multiply up to 4-digit numbers by single-digit and 2-digit numbers.

Children develop column methods with an understanding of place value, and they continue to use the key skill of unitising to multiply and divide by 10, 100 and 1,000.

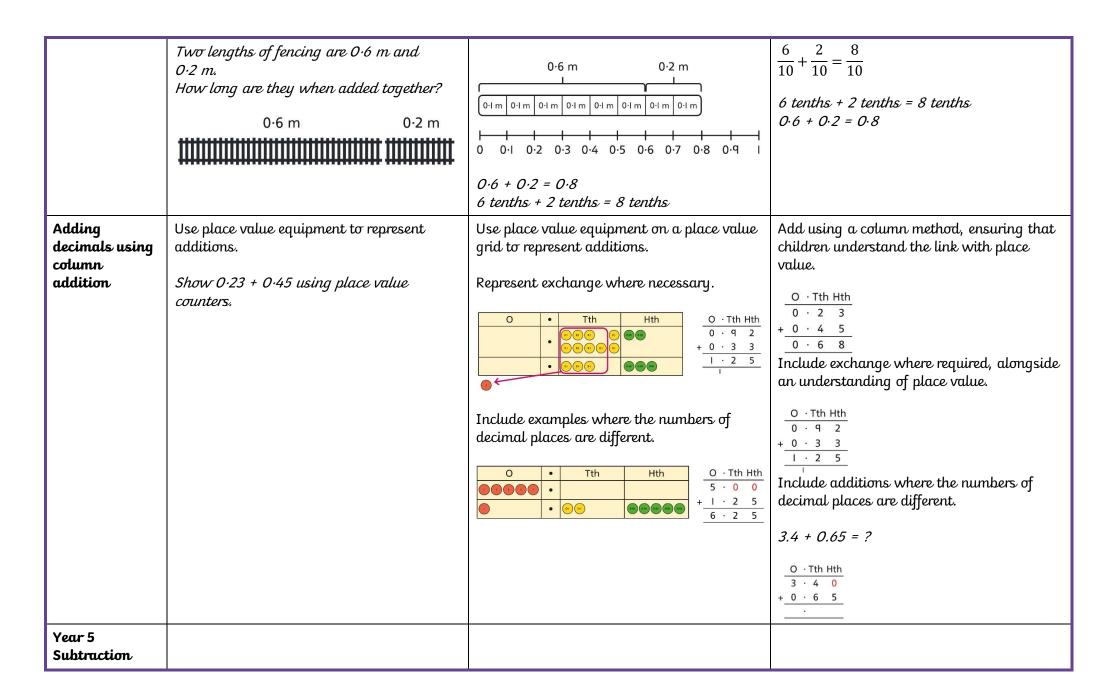
Written division methods are introduced and adapted for division by single-digit and 2-digit numbers and are understood alongside the area model and place value. In Year 6, children develop a secure understanding of how division is related to fractions.

Multiplication and division of decimals are also introduced and refined in Year 6.

Fractions: Children find fractions of amounts, multiply a fraction by a whole number and by another fraction, divide a fraction by a whole number, and add and subtract fractions with different denominators. Children become more confident working with improper fractions and mixed numbers and can calculate with them. Understanding of decimals with up to 3 decimal places is built through place value and as fractions, and children calculate with decimals in the context of measure as well as in pure arithmetic.

Children develop an understanding of percentages in relation to hundredths, and they understand how to work with common percentages: 50%, 25%, 10% and 1%.

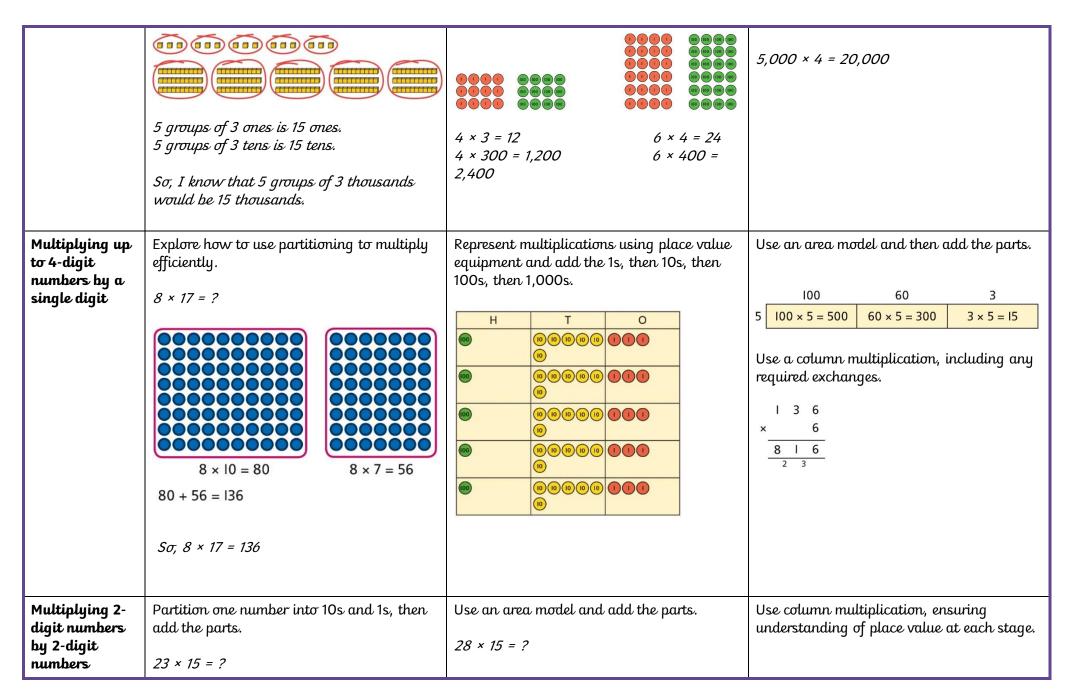
|  | Year 5   |  |  |  |  |  |
|--|--|--|--|--|--|--|
|  | Concrete   | Pictorial  | Abstract   |  |  |  |
| Year 5<br>Addition                       |  |  |  |  |  |  |
| Column<br>addition with<br>whole numbers | Use place value equipment to represent additions.  Add a row of counters onto the place value grid to show 15,735 + 4,012. | Represent additions, using place value equipment on a place value grid alongside written methods.   TTh Th Th H T O  2 0 1 5 3  + 1 9 1 7 5  3 9 3 2 8 | Use column addition, including exchanges.    Th Th H T O                   |  |  |  |
| Representing<br>additions                |  | Bar models represent addition of two or more numbers in the context of problem solving. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$         | Use approximation to check whether answers are reasonable.    TTh Th H T O |  |  |  |
| Adding tenths                            | Link measure with addition of decimals.  | Use a bar model with a number line to add tenths.  | Understand the link with adding fractions.                                 |  |  |  |

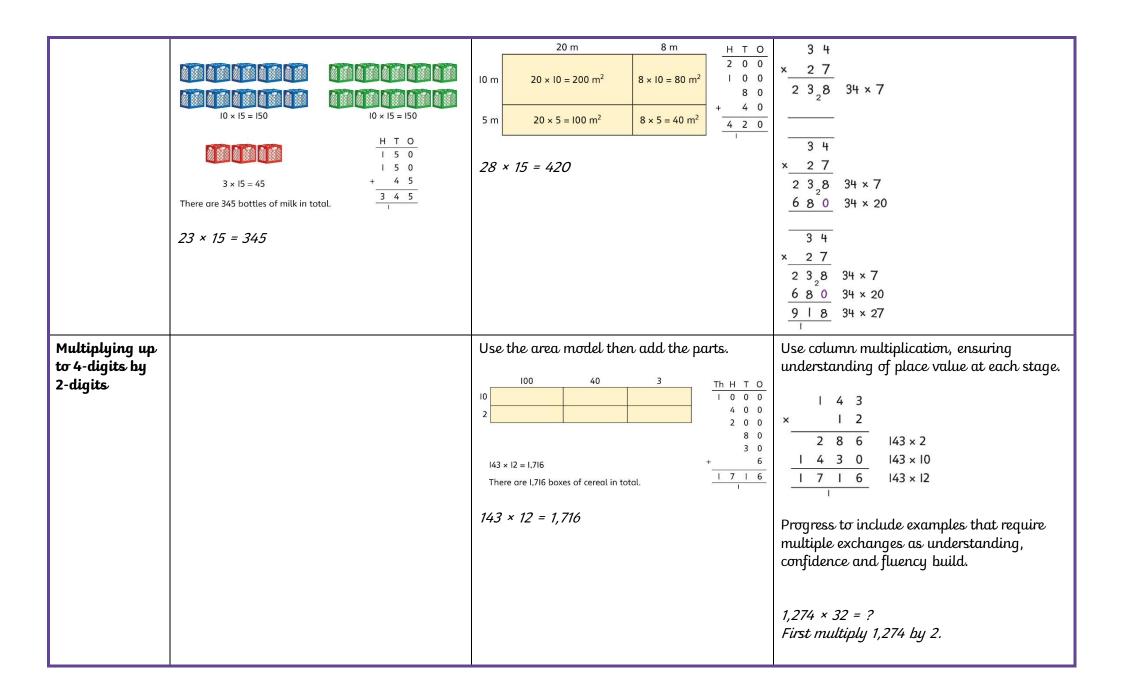


|                |   |   | 1  |
|----------------|---|---|--|
| Column         | Use place value equipment to understand | Represent the stages of the calculation using         | Use column subtraction methods with      |
| subtraction    | where exchanges are required.           | place value equipment on a grid alongside             | exchange where required.                 |
| with whole     | J ,                                     | the calculation, including exchanges where            | ,  |
| numbers        | 2,250 – 1,070                           | required.   | TTh Th H T O                             |
|                |   |   | <sup>5</sup> 8 "2 ' 0 9 7                |
|                |   | <i>15,735 - 2,582 = 13,153</i>                        | - I 8 5 3 4                              |
|                |   | .5,765 2,662 7.5,765                                  | 4 3 5 6 3                                |
|                |   | TTh Th H T O TTh Th H T O                             |  |
|                |   | 1 5 7 3 5<br>- 2 5 8 2                                | 62,097 - 18,534 = 43,563                 |
|                |   | - 2 5 6 2   | 12,221                                   |
|                |   | Now subtract the IOs. Exchange I hundred for IO tens. |  |
|                |   | TTh Th H T O TTh Th H T O                             |  |
|                |   | 1 5 % 1 3 5   |  |
|                |   | 5 3   |  |
|                |   | Subtract the 100s, 1,000s and 10,000s.                |  |
|                |   | TTh Th H T O T Th Th H T O I 5 7 3 5                  |  |
|                |   | 1 5 7 3 5<br>- 2 5 8 2<br>1 3 1 5 3                   |  |
|                |   | 1 3 1 5 3   |  |
| Checking       |   | Bar models represent subtractions in                  | Children can explain the mistake made    |
| strategies and |   | problem contexts, including 'find the                 | when the columns have not been ordered   |
| representing   |   | difference'.  | correctly.                               |
| subtractions   |   | ayja a wa i   | - comesay.                               |
|                |   | Athletics Stadium 75,450                              | Bella's working Correct method           |
|                |   | Attitutes studium 75,430                              | TTh Th H T O                             |
|                |   | Hockey Centre ← 42,300                                | + 4 0 1 2 + 4 0 1 2                      |
|                |   | Velodrome (15,735) ← →                                | 5 7 9 9 7                                |
|                |   | 7   | Use approximation to check calculations. |
|                |   |   | 11                                       |
|                |   |   | I calculated 18,000 + 4,000 mentally tσ  |
|                |   |   | check my subtraction.                    |
|                |   |   | 3  |
| Choosing       |   |   | To subtract two large numbers that are   |
| efficient      |   |   | close, children find the difference by   |
| methods        |   |   | counting on.                             |
|                |   |   | 2,002 - 1,995 = ?                        |
|                |   |   |  |

| Subtracting              | Explore complements to a whole number by                          | Use a place value grid to represent the                                | Use addition to check subtractions.  I calculated 7,546 - 2,355 = 5,191.  I will check using the inverse.  Use column subtraction, with an |
|--------------------------|---|--|--|
| decimals                 | working in the context of length.                                 | stages of column subtraction, including exchanges where required.      | understanding of place value, including subtracting numbers with different numbers   |
|                          | 0.49 m ]  | 5.74 - 2.25 = ?  | of decimal places.  3.921 - 3.75 = ?   |
|                          | I m – m   | 0 • Tth Hth 5 · 7 · 4  | O · Tth Hth Thth   |
|                          | 1 - 0.49 = ?  | Exchange I tenth for I0 hundredths.                                    | 3 · 9 2 I<br>- 3 · 7 5 0   |
|                          |   | 0 Tth Hth 5 · 67 ' 14 - 2 · 2 · 5                                      | •  |
|                          |   | Now subtract the 5 hundredths.   |  |
|                          |   | O Tth Hth  ○○○○○○○ ○○○○○ ○○○○○ ○○○○○ ○○○○○ ○○○○○ ○○○○                  |  |
|                          |   | Now subtract the 2 tenths, then the 2 ones.  O Tth Hth                 |  |
|                          |   | 3 · 4 · q  |  |
| Year 5<br>Multiplication |   |  |  |
| Understanding factors    | Use cubes or counters to explore the meaning of 'square numbers'. | Use images to explore examples and non-<br>examples of square numbers. | Understand the pattern of square numbers in the multiplication tables.   |

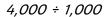
|   | 25 is a square number because it is made from 5 rows of 5.  Use cubes to explore cube numbers.  8 is a cube number:   | 8 × 8 = 64 8 <sup>2</sup> = 64  12 is not a square number, because you cannot multiply a whole number by itself to make 12. | Use a multiplication grid to circle each square number. Can children spot a pattern?  |
|---|---|---|---|
| Multiplying by<br>10, 100 and<br>1,000              | Use place value equipment to multiply by 10, 100 and 1,000 by unitising. $ \frac{4 \times 1 = 4 \text{ ones} = 4}{4 \times 10 = 4 \text{ tens} = 40} $ $ \frac{4 \times 100 = 4 \text{ hundreds}}{4 \times 100} $ | Understand the effect of repeated multiplication by 10.   | Understand how exchange relates to the digits when multiplying by 10, 100 and 1,000.  H T O T $17 \times 10 = 170$ $17 \times 100 = 17 \times 10 \times 10 = 1,700$ $17 \times 1,000 = 17 \times 10 \times 10 \times 10 = 17,000$ |
| Multiplying by<br>multiples of 10,<br>100 and 1,000 | Use place value equipment to explore multiplying by unitising.  | Use place value equipment to represent how to multiply by multiples of 10, 100 and 1,000.                                   | Use known facts and unitising to multiply.  5 × 4 = 20  5 × 40 = 200  5 × 400 = 2,000  5 × 4,000 - 20,000   |



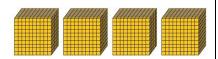


|   | I   | I   |   |
|---|---|---|---|
|   |   |   | $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$  |
| Multiplying<br>decimals by 10,<br>100 and 1,000 | Use place value equipment to explore and understand the exchange of 10 tenths, 10 hundredths or 10 thousandths. | Represent multiplication by 10 as exchange on a place value grid.  Order Tth Hth Hth Graph of the second of the s | Understand how this exchange is represented on a place value chart.  The Heat Toology Telephone |
| Year 5<br>Division                              |   |   |   |

| Understanding<br>factors and<br>prime numbers   | Use equipment to explore the factors of a given number.   | Understand that prime numbers are numbers with exactly two factors.  | Understand how to recognise prime and composite numbers.   |
|---|---|--|--|
|   | 24 ÷ 3 = 8<br>24 ÷ 8 = 3<br>8 and 3 are factors of 24 because they divide 24 exactly.<br>24 ÷ 5 = 4 remainder 4.<br>5 is not a factor of 24 because there is a remainder.   | 13 ÷ 1 = 13<br>13 ÷ 2 = 6 r 1<br>13 ÷ 4 = 4 r 1<br>1 and 13 are the only factors of 13.<br>13 is a prime number.     | I know that 31 is a prime number because it can be divided by only 1 and itself without leaving a remainder.  I know that 33 is not a prime number as it can be divided by 1, 3, 11 and 33.  I know that 1 is not a prime number, as it has only 1 factor.   |
| Understanding inverse operations and the link with multiplication, grouping and sharing | Use equipment to group and share and to explore the calculations that are present.  I have 28 counters.  I made 7 groups of 4. There are 28 in total.  I have 28 in total. I shared them equally into 7 groups. There are 4 in each group.  I have 28 in total. I made groups of 4. There are 7 equal groups. | Represent multiplicative relationships and explore the families of division facts. $60 \div 4 = 15$ $60 \div 15 = 4$ | Represent the different multiplicative relationships to solve problems requiring inverse operations. $\begin{vmatrix} 2 & + 3 & = \\ 2 & + 3 & = \end{vmatrix} $ Understand missing number problems for division calculations and know how to solve them using inverse operations. $22 \div ? = 2$ $22 \div 2 = ?$ $? \div 22 = 2$ |
| Dividing whole<br>numbers by 10,<br>100 and 1,000                                       | Use place value equipment to support unitising for division.  | Use a bar model to support dividing by unitising.  | Understand how and why the digits change on a place value grid when dividing by 10, 100 or 1,000.  |







4,000 is 4 thousands.

4 × 1,000= 4,000

Sσ, 4,000 ÷ 1,000 = 4

| 380 | ÷ | 10 | = 38 |
|-----|---|----|------|
|-----|---|----|------|

| _ |   |   |   |   |   |   | _ |   |   |
|---|---|---|---|---|---|---|---|---|---|
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |



| 380 is 38 | tens. |
|-----------|-------|
| 38 × 10 = | 380   |
| 10 x 38 = | 380   |

So, 380 ÷ 10 = 38

| Th | Н | Т | 0 |
|----|---|---|---|
| 3  | 2 | 0 | 0 |

3,200 ÷ 100 = ?

3,200 is 3 thousands and 2 hundreds.

200 ÷ 100 = 2

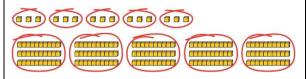
3,000 ÷ 100 = 30

3,200 ÷ 100 = 32

So, the digits will move two places to the right.

## Dividing by multiples of 10, 100 and 1,000

Use place value equipment to represent known facts and unitising.



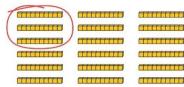
15 ones put into groups of 3 ones. There are 5 groups.

15 ÷ 3 = 5

15 tens put into groups of 3 tens. There are 5 groups.

150 ÷ 30 = 5

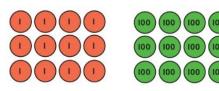
Represent related facts with place value equipment when dividing by unitising.



180 is 18 tens.

18 tens divided into groups of 3 tens. There are 6 groups.

180 ÷ 30 = 6



Reason from known facts, based on understanding of unitising. Use knowledge of the inverse relationship to check.

3,000 ÷ 5 = 600

3,000 ÷ 50 = 60

3,000 ÷ 500 = 6

5 × 600 = 3,000

50 × 60 = 3,000

500 × 6 = 3,000

| Dividing up to  | Evolute a marking using place value  | 12 ones divided into groups of 4. There are 3 groups.  12 hundreds divided into groups of 4 hundreds. There are 3 groups.  1200 ÷ 400 = 3  | Lloo about division for up to / digit numbers   |
|---|--|--|---|
| Dividing up to four digits by a single digit using short division | Explore grouping using place value equipment.  268 ÷ 2 = ?  There is 1 group of 2 hundreds. There are 3 groups of 2 tens. There are 4 groups of 2 ones.  264 ÷ 2 = 134 | Use place value equipment on a place value grid alongside short division.  The model uses grouping.  A sharing model can also be used, although the model would need adapting.   TOO  A 4 4 8 TOO  A 5 TOO  A 6 TOO  A 6 TOO  A 7 TOO  A 7 TOO  A 6 TOO  A 7 TOO  A 7 TOO  A 7 TOO  A 6 TOO  A 7 TOO  A 7 TOO  A 7 TOO  A 8 TOO  A 6 TOO  There is 1 group of 4 in 4 tens.  There are 2 groups of 4 in 8 ones.  Work with divisions that require exchange. | Use short division for up to 4-digit numbers divided by a single digit.  0 5 5 6 7 3 38 39 42  3,892 ÷ 7 = 556  Use multiplication to check.  556 × 7 = ?  6 × 7 = 42  50 × 7 = 350  500 × 7 = 3500  3,500 + 350 + 42 = 3,892 |

|  |  | T O First, lay out the problem.  2 T O How many groups of 4 go into 9 tens? 2 groups of 4 tens with 1 ten left over.  2 T O Exchange the 1 ten left over for 10 ones.  We now have I2 ones.  4 9 12 T O How many groups of 4 go into 9 tens?  2 groups of 4 tens with 1 ten left over for 10 ones.  We now have I2 ones.  3 groups of 4 ones.            |  |
|--|--|--|--|
| Understanding<br>remainders                  | Understand remainders using concrete versions of a problem.  80 cakes divided into trays of 6.  80 cakes in total. They make 13 groups of 6, with 2 remaining. | Use short division and understand remainders as the last remaining 1s.  Lay out the problem as short division.  Lay out the problem as short division.  How many groups of 6 go into 8 tens? There is I group of 6 tens. There are 2 tens remaining.  There are 3 groups of 6 go into 20 ones? There are 3 groups of 6 ones. There are 2 ones remaining. | In problem solving contexts, represent divisions including remainders with a bar model. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ |
| Dividing<br>decimals by 10,<br>100 and 1,000 | Understand division by 10 using exchange.  2 ones are 20 tenths.   | Represent division using exchange on a place value grid.   | Understand the movement of digits on a place value grid.   |

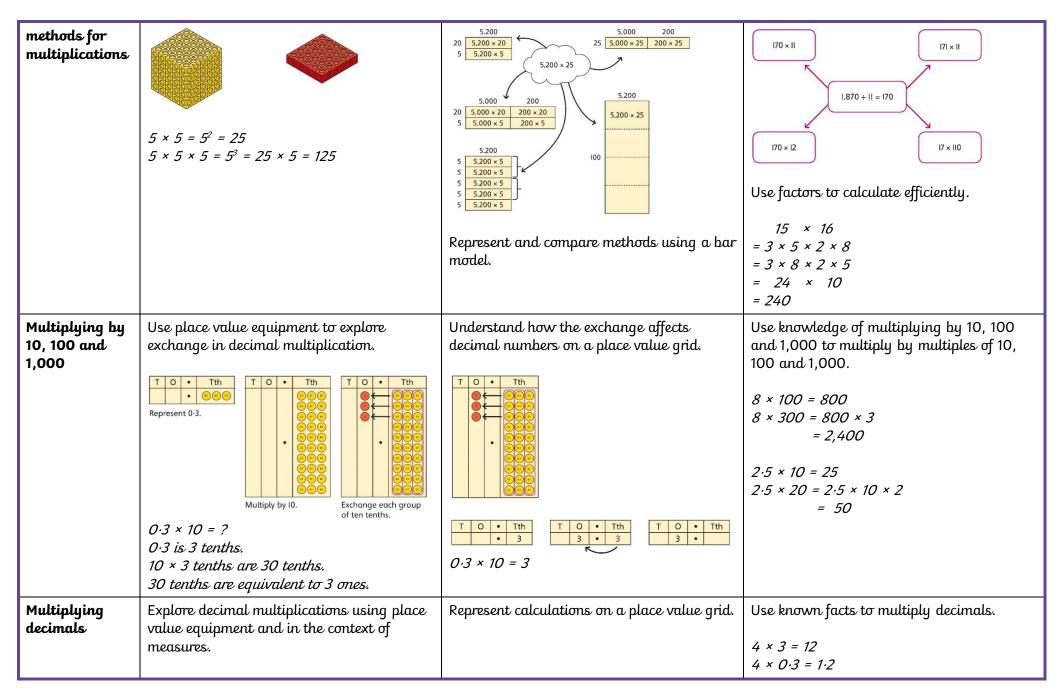
|   | 20 tenths divided by 10 is 2 tenths.  | 1.5 is 1 one and 5 tenths. This is equivalent to 10 tenths and 50 hundredths. 10 tenths divided by 10 is 1 tenth. 50 hundredths divided by 10 is 5 hundredths. 1.5 divided by 10 is 1 tenth and 5 hundredths. 1.5 ÷ 10 = 0.15 | O       Tth       Hth       Thth         0       8       5         0       38       35         0       70       38       35         0       70       70       70         0       70       70       70         0       70       70       70         8       70       70       70         8       70       70       70         8       70       70       70         8       70       70       70         8       70       70       70         8       70       70       70         8       70       70       70         8       70       70       70         8       70       70       70         8       70       70       70         8       70       70       70         8       70       70       70         9       8       70       70         9       8       70       70         9       8       70       70         9       8       70       70 |
|---|---|---|--|
| Understanding<br>the relationship<br>between<br>fractions and<br>division | Use sharing to explore the link between fractions and division.  1 whole shared between 3 people. Each person receives one-third. | Use a bar model and other fraction representations to show the link between fractions and division. $I \div 3 = \frac{1}{3}$  | Use the link between division and fractions to calculate divisions. $5 \div 4 = \frac{5}{4} = 1\frac{1}{4}$ $11 \div 4 = \frac{11}{4} = 2\frac{3}{4}$  |
|   |   | Year 6  |  |
|   | Concrete  | Pictorial   | Abstruct   |

| Year 6<br>Addition                                   |   |  |   |  |
|--|---|--|---|--|
| Comparing and selecting efficient methods            | Represent 7-digit numbers on a place value grid, and use this to support thinking and mental methods.  M HTh TTh Th H T O | Discuss similarities and differences between methods, and choose efficient methods based on the specific calculation.  Compare written and mental methods alongside place value representations.  The The Heart Compares with the specific calculation and the specific calculation.  The The Heart Compares with the specific calculation and the specific calculation.  The The Heart Compares with the specific calculation and the specific calculation.  The The Heart Compares with the specific calculation.  The The The Heart Compares with the specific calculation.  The The The Heart Compares with the specific calculation and the specific calculation with the specific calculation with the specific calculation and the specific calculation with the specific cal | Use column addition where mental methods are not efficient. Recognise common errors with column addition.  32,145 + 4,302 = ?  TTh Th H T O |  |
| Selecting<br>mental<br>methods for<br>larger numbers | Represent 7-digit numbers on a place value grid, and use this to support thinking and mental methods.                     | Use a bar model to support thinking in addition problems.  257,000 + 99,000 = ?  | Use place value and unitising to support mental calculations with larger numbers. $195,000 + 6,000 = ?$                                     |  |

| where<br>appropriate                                       | 2,411,301 + 500,000 = ?  This would be 5 more counters in the HTh place.  So, the total is 2,911,301.  2,411,301 + 500,000 = 2,911,301   | f 257,000 f 100,000  I added 100 thousands then subtracted 1 thousand.  257 thousands + 100 thousands = 357 thousands  257,000 + 100,000 = 357,000  357,000 - 1,000 = 356,000  So, 257,000 + 99,000 = 356,000 | 195 + 5 + 1 = 201  195 thousands + 6 thousands = 201 thousands  Sσ, 195,000 + 6,000 = 201,000  |  |  |  |
|--|--|---|--|--|--|--|
| Understanding<br>order of<br>operations in<br>calculations | Use equipment to model different interpretations of a calculation with more than one operation. Explore different results. $3 \times 5 - 2 = ?$ | Model calculations using a bar model to demonstrate the correct order of operations in multi-step calculations. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$  | Understand the correct order of operations in calculations without brackets.  Understand how brackets affect the order of operations in a calculation. $4 + 6 \times 16$ $4 + 96 = 100$ $(4 + 6) \times 16$ $10 \times 16 = 160$ |  |  |  |
| Year 6<br>Subtraction                                      |  |   |  |  |  |  |
| Comparing and selecting                                    | Use counters on a place value grid to represent subtractions of larger numbers.  | Compare subtraction methods alongside place value representations.  | Compare and select methods.  |  |  |  |

| efficient<br>methods                           | Th H T O                                  | Th H T O  2 6 7 9  - 5 3 4  2 1 4 5  Use a bar model to represent calculations, including 'find the difference' with two bars as comparison.  computer game  puzzle book  fil2-50                       | Use column subtraction when mental methods are not efficient.  Use two different methods for one calculation as a checking strategy. $ \frac{Th}{1} \frac{H}{8H} \frac{T}{10} \frac{O}{1} \frac{+6}{8H} \frac{-400}{1} $ Use column subtraction for decimal problems, including in the context of measure. $ \frac{H}{3} \frac{T}{0} \frac{O}{1} \cdot \frac{T}{1} \cdot \frac{H}{1} \cdot \frac{H}{1} $ $ \frac{H}{3} \frac{T}{0} \cdot \frac{O}{1} \cdot \frac{T}{1} \cdot \frac{H}{1} \cdot \frac{H}{1} $ $ \frac{H}{3} \frac{T}{0} \cdot \frac{O}{1} \cdot \frac{O}{1} \cdot \frac{O}{1} \cdot \frac{O}{1} $ |
|--|---|---|--|
| Subtracting<br>mentally with<br>larger numbers |   | Use a bar model to show how unitising can support mental calculations.  950,000 - 150,000  That is 950 thousands - 150 thousands  950  So, the difference is 800 thousands. 950,000 - 150,000 = 800,000 | Subtract efficiently from powers of 10.  10,000 - 500 = ?  |
| Year 6<br>Multiplication                       |   | 750,000 - 150,000 - 800,000   |  |
| Multiplying up<br>to a 4-digit                 | Use equipment to explore multiplications. | Use place value equipment to compare methods.   | Understand area model and short multiplication.  |

| number by a<br>single digit<br>number                            | Th H T O  4 groups of 2,345  This is a multiplication:  4 × 2,345 2,345 × 4 | Method I    3 2 2 5     3 2 2 5     3 2 2 5     3 2 2 5     3 2 2 5     4 3 2 2 5     1 2 9 0 0     1 1 2      Method 2     4 × 3,000 4 × 200 4 × 20 4 × 5     12,000 + 800 + 80 + 20 =  2,900 | Compare and select appropriate methods for specific multiplications.  Method 3  3.000 200 20 5 4 12.000 800 80 20  12.000 + 800 + 80 + 20 = 12.900  Method 4  3 2 2 5  × 4  1 2 9 0 0  1 2 |
|--|---|--|--|
| Multiplying up<br>to a 4-digit<br>number by a<br>2-digit number  |   | Use an area model alongside written multiplication.  Method I    1,000   200   30   5     20   20,000   4,000   600   100     1,000   200   30   5      1   2   3   5     ×                    | Use compact column multiplication with understanding of place value at all stages.    1 2 3 5  |
| Using<br>knowledge of<br>factors and<br>partitions to<br>compare | Use equipment to understand square numbers and cube numbers.                | Compare methods visually using an area model. Understand that multiple approaches will produce the same answer if completed accurately.  | Use a known fact to generate families of related facts.  |



| Year 6 |   |   | 0·02 × 3   |                            |                  |        | •   |        |            |         |
|--------|---|---|--|----------------------------|------------------|--------|-----|--------|------------|---------|
|        |   |   | 0·2 × 3  |                            |                  | 0      | •   | 6      |            |         |
|        |   |   | 2 × 3  |                            |                  | 6      |     |        |            |         |
|        |   |   | Use a pla<br>effects of                            |                            |                  |        |     |        | and th     | ie<br>] |
|        | $4 \times 1 \text{ cm} = 4 \text{ cm}$<br>$4 \times 0.3 \text{ cm} = 1.2 \text{ cm}$<br>$4 \times 1.3 = 4 + 1.2 = 5.2 \text{ cm}$ | T 0 • Tth • 0.2 +0.2 +0.2 +0.2 0  | 1·8 × 4 =<br>18 × 0·4<br>180 × 0·<br>18 × 0·0      | = ?<br>k = ?<br>·4 = ?     | 2                |        |     |        |            |         |
|        | → → → → → → → → → → → → → → → → → → →   | Understand the link between multiplying decimals and repeated addition. | I know t<br>This can                               |                            |                  |        |     |        |            |         |
|        | 3 groups of 4 tenths is 12 tenths. 4 groups of 3 tenths is 12 tenths.   | $3 \times 0.3 = 0.9$ T  O  Th  O  O  O  O  O  O  O  O  O  O  O  O  O    | 20 × 5 = 20 × 0.0<br>20 × 0.0<br>Find fammultiplic | 5 = 10<br>95 = 1<br>rilies | )<br>1<br>of fac | ts fro | m a | , knov | <b>v</b> n |         |
|        | 0-1 0-1 0-1   | 3 × 3 = 9   | 4 × 0·03   | 3 = O                      | ·12              |        |     |        |            |         |

Division

| Understanding<br>factors   | Use equipment to explore different factors of a number.                                       | Recognise prime numbers as numbers having exactly two factors. Understand the link with division and remainders.       | Recognise and know primes up to 100. Understand that 2 is the only even prime, and that 1 is not a prime number.                              |
|----------------------------|---|--|---|
|                            | $24 \div 4 = 6$ $30 \div 4 = 7$ remainder 2<br>4 is a factor of 24 but is not a factor of 30. | 17 ÷ 2 = 8 r l   | 1) 12 (3) 14 15 16 (7) 18 (19 20<br>21 22 (23) 24 25 26 27 28 (29 30  |
| Dividing by a single digit | Use equipment to make groups from a total.  | H T O Groups of 6 are in 100?  How many groups of 6 are in 100?  How many groups of 6 are in 13 tens?  O 2 6   1 '3 '2 | Use short division to divide by a single digit.   |
|                            | There are 78 in total. There are 6 groups of 13. There are 13 groups of 6.                    | H T O How many groups of 6 are in 12 ones? 6 1 1 3 12  | 0 2<br>6   1   3   2<br>6   1   3   2   |
|                            |   |  | Use an area model to link multiplication and division.  |
|                            |   |  | ? $10 	 10 	 1 	 1$ 6 $132 	 6 	 60 	 60 	 60 	 6 	 6$ 6 $\times$ ? = $132 	 20 	 2$ 6 $120 	 12$ $132 = 120 + 12$ $132 \div 6 = 20 + 2 = 22$ |

| Dividing by a<br>2-digit number<br>using factors | Understand that division by factors can be used when dividing by a number that is not prime.     | Use factors and repeated division.  1,260 ÷ 14 = ?  1,260                            | Use factors and repeated division where appropriate. $2,100 \div 12 = ?$ $2,100 \rightarrow                                  $   |
|--|--|--|--|
| Dividing by a 2-digit number using long division | Use equipment to build numbers from groups.  182 divided into groups of 13. There are 14 groups. | Use an area model alongside written division to model the process.  377 ÷ 13 = ?  13 | Use long division where factors are not useful (for example, when dividing by a 2-digit prime number).  Write the required multiples to support the division process. $377 \div 13 = ?$ $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ |

| Dividing by 10,<br>100 and 1,000 | Use place value equipment to explore division as exchange.  Divide 20 counters by 10.  0.2 is 2 tenths. 2 tenths is equivalent to 20 hundredths. | Represent division to show the relationship with multiplication. Understand the effect of dividing by 10, 100 and 1,000 on the digits on a place value grid. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ | $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$             |
|----------------------------------|--|---|--|
|                                  | 20 hundredths divided by 10 is 2 hundredths.   |   | Sσ, 40 ÷ 50 = 0·8  |
| Dividing<br>decimals             | Use place value equipment to explore division of decimals.   | Use a bar model to represent divisions.   | Use short division to divide decimals with up to 2 decimal places. |



8 tenths divided into 4 groups. 2 tenths in each group.

| 0.8 |   |   |   |  |  |
|-----|---|---|---|--|--|
| ?   | ? | ? | ? |  |  |

 $4 \times 2 = 8$ 

 $8 \div 4 = 2$ 

So,  $4 \times 0.2 = 0.8$ 

 $0.8 \div 4 = 0.2$ 

|   |   | • |   |   |
|---|---|---|---|---|
| 8 | 4 | • | 2 | 4 |

0 · 8 4 · <sup>4</sup>2 4

 $0 \cdot 5 \ 3$